ASSIGNMENT SET-I

Department of Mathematics

Mugberia Gangadhar Mahavidyalaya



B.Sc Hon.(CBCS)

Mathematics: Semester-IV

Paper Code: SEC-2T

[Graph Theory]

Answer all the questions

- 1. Define graph.
- 2. Define self loop and parallel edge in a graph.
- 3. Define simple graph.
- 4. Define incidence and degree.
- 5. Define isolated vertex and pendant vertex and null graph.
- 6. State and proof hand shaking lemma.
- 7. Define isomorphic graph with example.
- 8. Define sub graph and its compliment.
- 9. Define spanning sub graph, edge disjoin sub graph, vertex disjoint sub graph.
- 10. Define self complementary graph.
- 11. Prove that in a self complementary the no of vertices has 4k or 4k+1.
- 12. Show that the maximum number of edges in a simple graph with in n vertices is $\frac{n(n-1)}{2}$.
- 13. Can a graph with eleven vertices be isomorphic to its complement?
- 14. Prove that a simple graph G with at least two vertices contain two vertices of same degree.
- 15. What is the maximum number of vertices in a graph with 41 edges and all the vertices at least degree three?
- 16. Define walk, path and circuits.
- 17. What is the length of a path?
- 18. Define connected and disconnected graph.

- 19. Prove that in a simple graph with n vertices and K components can have most $\frac{(n-K)(n-K+1)}{2}$ edges.
- 20. If a simple graph G with n vertices has more than $\frac{(n-2)(n-1)}{2}$ edges, then prove that G is connected.
- 21. Define intersection, union and ring sum of two graph.
- 22. Define decomposition of a graph.
- 23. Define complete and regular graph.
- 24. Define cycle, path and wheel graph.
- 25. Define bipartite graph and complete bipartite graph.
- 26. Show that maximum number of edges in complete bipartite graph of n vertices is $\frac{n^2}{4}$
- 27. What is the sum of the degree of the vertices of three regular graphs with n vertices?
- 28. Which of the platonic graphs have Hamiltonian circuits?
- 29. Which complete bipartite graphs are Hamiltonian as well as Eulerian?
- 30. For which values of n is the wheel W_n Hamiltonian?
- 31. Prove that if **G** is a bipartite graph with an odd number of vertices then **G** is not Hamiltonian?
- 32. Draw a graph that has both an Euler circuit and a Hamiltonian circuit
- 33. Draw a graph that has an Euler circuit but has no Hamiltonian circuit.
- 34. Draw a graph that has Hamiltonian circuit but has no Euler circuit.
- 35. Draw a graph that has Hamiltonian circuit but has no Euler circuit.
- 36. Draw a graph that has Hamiltonian circuit but has no Euler circuit.
- 37. Draw a graph that has neither an Euler circuit nor a Hamiltonian circuit.
- 38. Let G be bipartite graph with disjoint vertex sets V_1 an V_2 d. show that if G has a Hamiltonian circuit then V_1 and V_2 have the same number of elements.
- 39. Prove that a graph G with n vertices has a Hamiltonian path if the sum of the degree of every pair of vertices v_i and v_j in G satisfies the condition

$$d(\boldsymbol{v}_i) + d(\boldsymbol{v}_j) \ge n - 1$$

40. Show that the Petersen graph is non Hamiltonian.

